

Image Analysis

Rasmus R. Paulsen

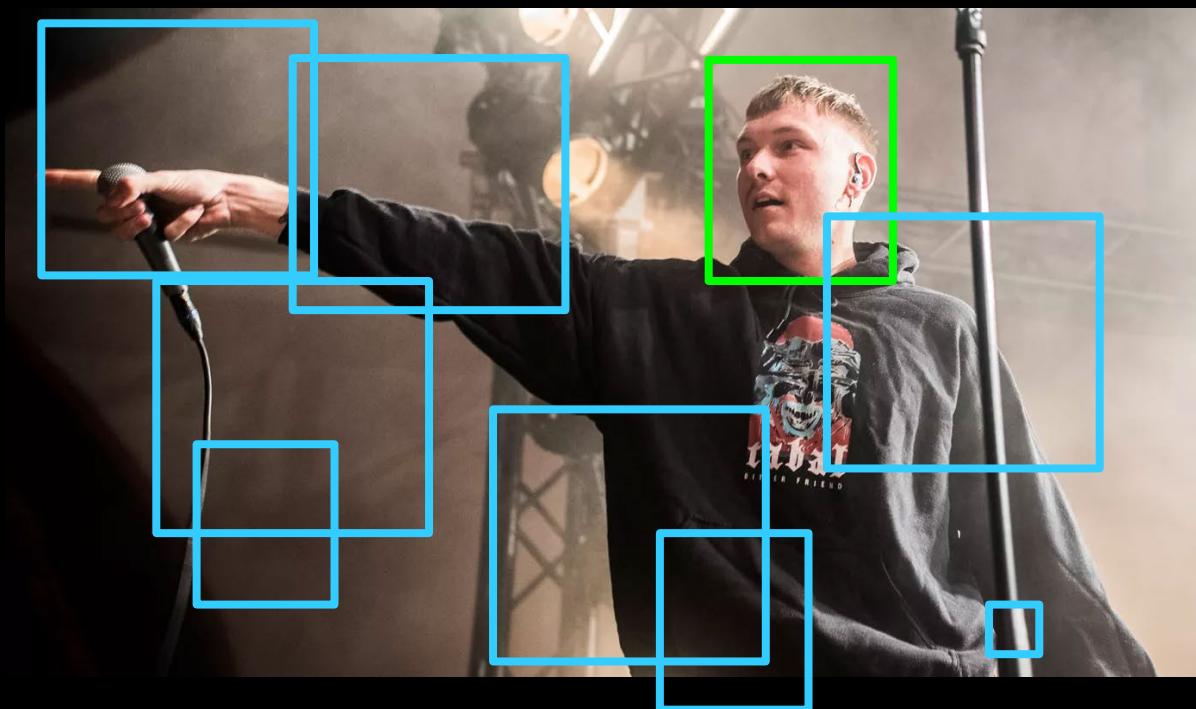
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Lecture 11 – Face detection using the Viola Jones method



What can you do after today?

- Describe the concept of face detection
- Describe the concept of Haar features
- Compute the values of 2, 3 and 4 rectangle Haar features
- Describe the integral image
- Compute the sum of pixels values in a rectangle using an integral image
- Describe the concept of a weak classifier
- Describe how several weak classifiers can be combined into a strong classifier
- Describe the attentional cascade
- Describe how faces can be detected using a moving window

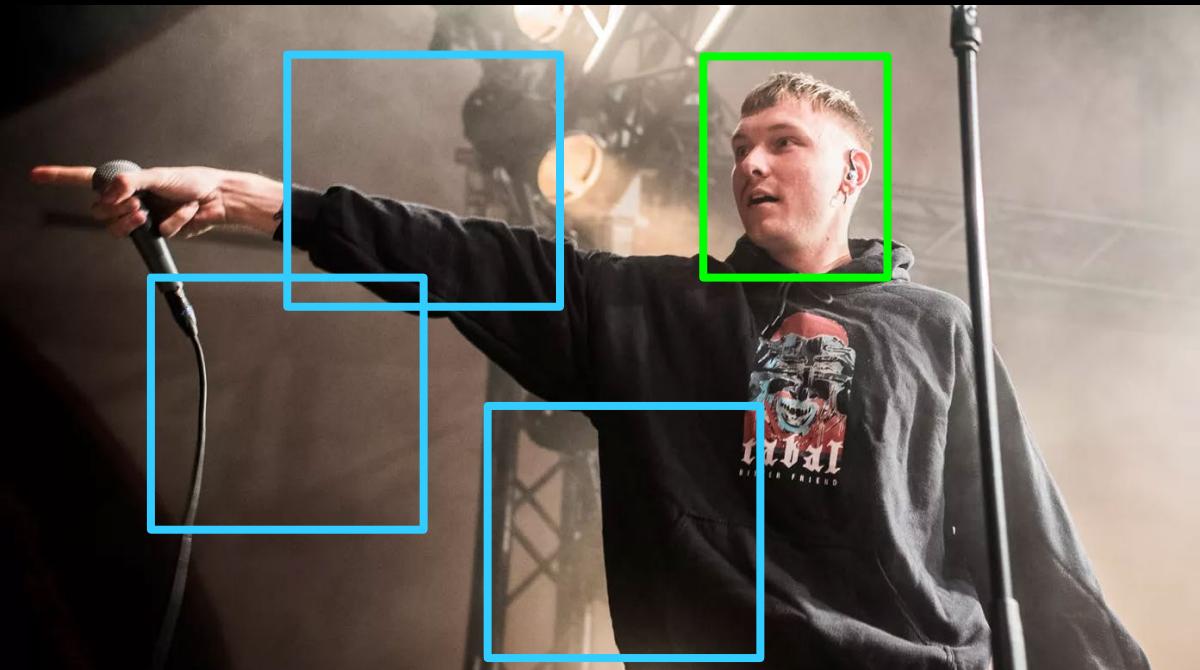
Face detection



■ First problem

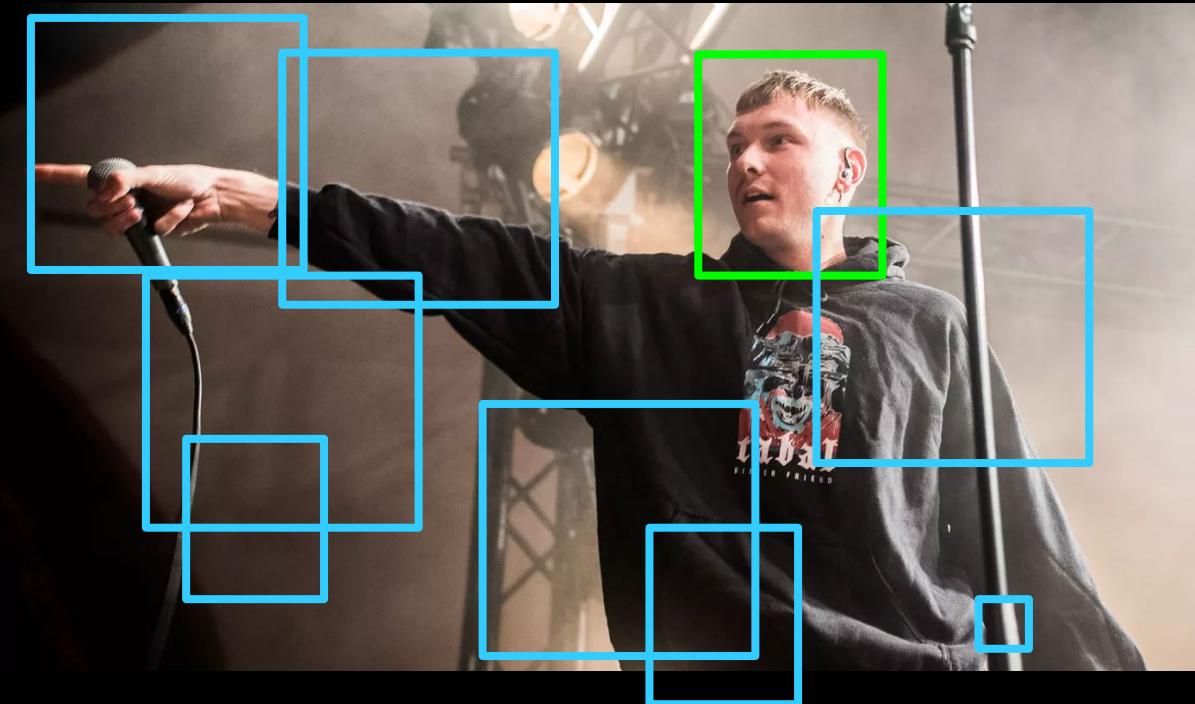
- Analyze a **window** in an image
- Is there a face in that window?

Face detection



- Slightly more advanced
 - Analyze many **windows** in an image
 - How many (if any) **windows** contain faces?

Face detection



■ Ideal

- Analyze (almost) all possible **windows** in an image
- How many (if any) **windows** contain faces?

What is needed?



- A fast method to determine if a *window* contains a face

Primary task – image feature based classification

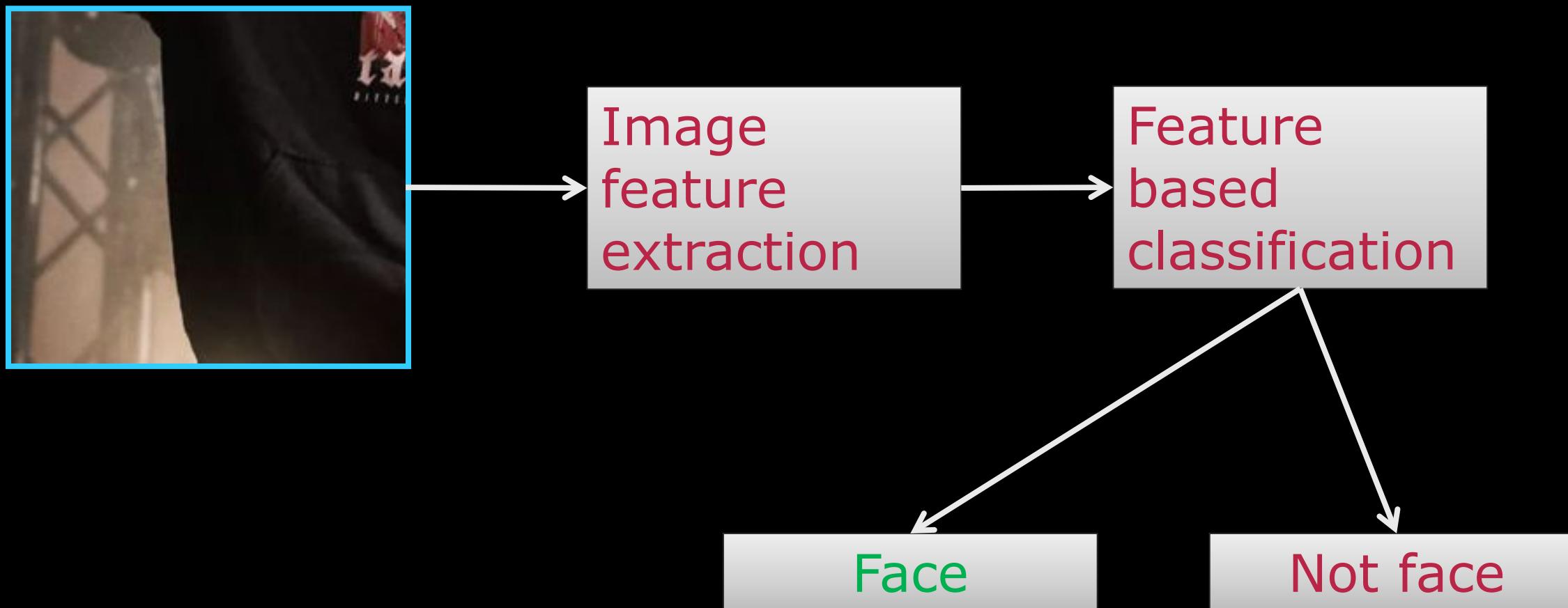


Image based features - what features can you think of?



symmetry
circularity
eye color differences
nose straight
lines pixelmetal
text values
difference eyes mouth haar
contrast shape
circles curves
poles contrasts

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Viola Jones – fast features and smart classification



Many image
features
very fast

Boosted
cascade
classifier

Face

Not face

Training data



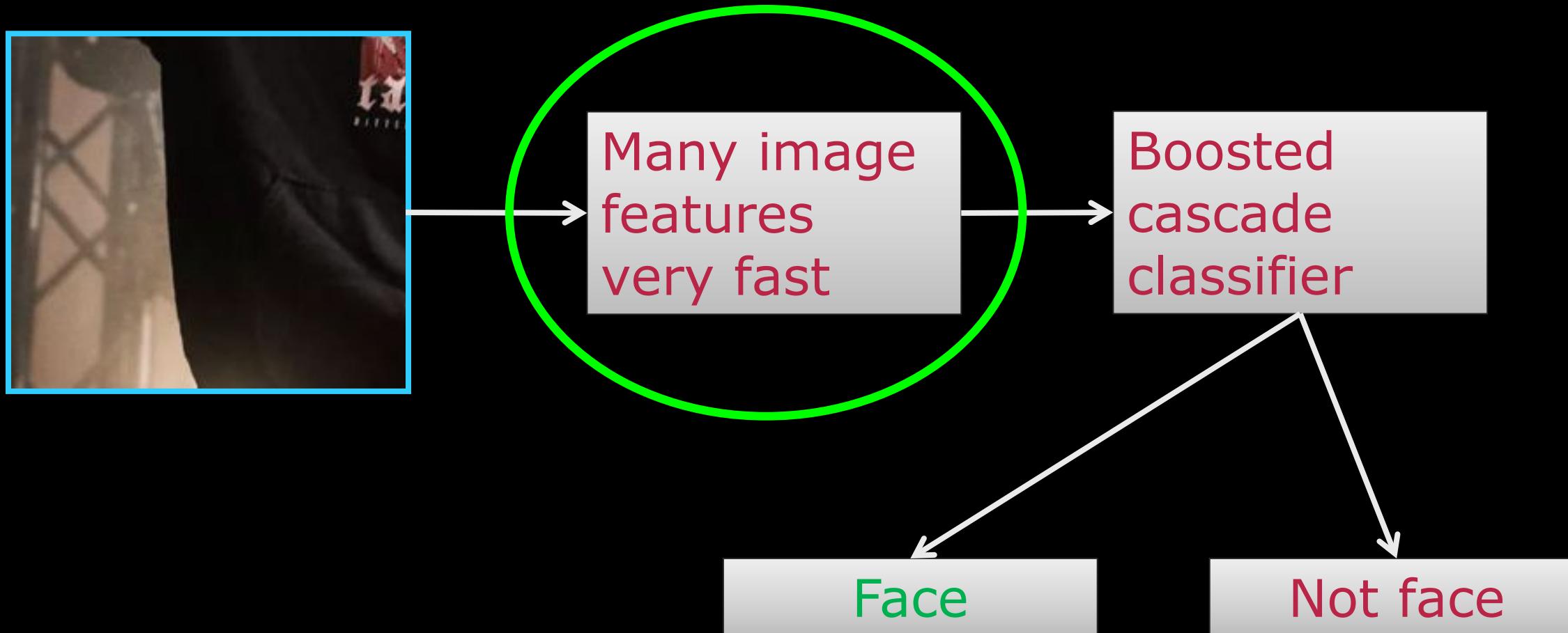
■ Face images:

- 4916 hand labelled faces
- Aligned and scaled to 24x24 pixels

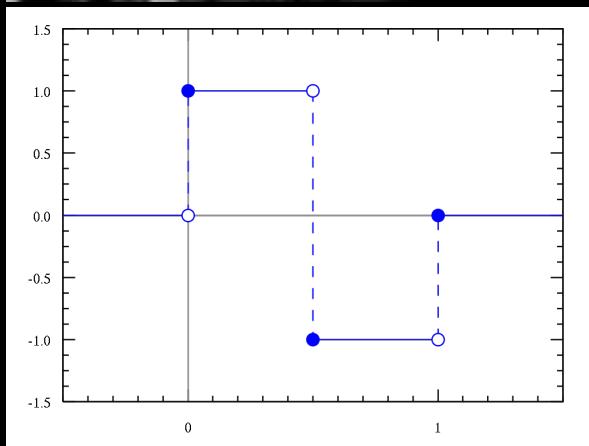
■ Non-face images:

- 9544 images with no faces
- 350 million sub-windows sampled from these

Viola Jones – fast features and smart classification



Haar features



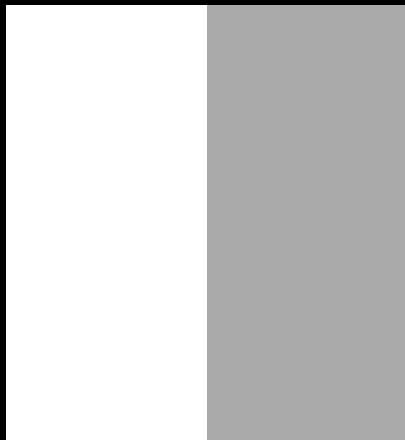
- Alfred Haar (1885-1933)
 - Hungarian Mathematician
- Introduced the Haar wavelet in 1909
- *A wavelet is a wave-like oscillation with an amplitude that begins at zero, increases or decreases, and then returns to zero one or more times.*
- Simplest possible wavelet

<https://en.wikipedia.org/wiki/Wavelet>

https://en.wikipedia.org/wiki/Haar_wavelet

Haar features

Two rectangle features



A

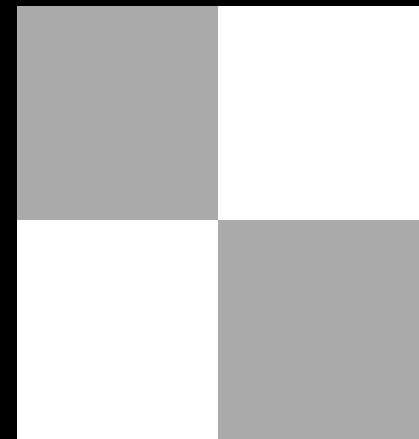
B

Three rectangle feature



C

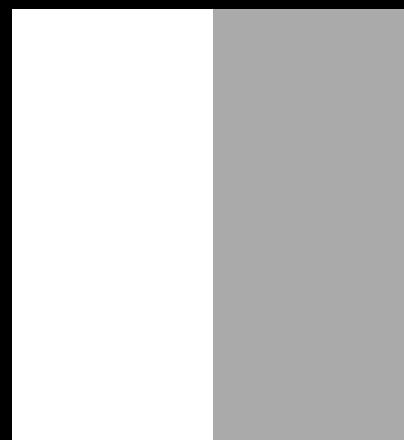
Four rectangle feature



D

$$\text{Feature} = \boxed{\text{Sum of pixel values in image}} - \boxed{\text{Sum of pixel values in image}}$$

One Haar feature



A

3	42	115	137	1	66
86	154	21	254	198	204
41	67	58	20	208	110
203	167	233	113	222	232
79	176	39	27	22	46
135	191	211	245	102	67

$$\text{Feature} = 254 + 198 + 20 + 208 + 113 + 222 - 154 - 21 - 67 - 58 - 167 - 233 = 1015 - 700 = 315$$

Four rectangle Haar feature - what is the feature value?

567

179

-611

-113

76

I do not know

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Four rectangle Haar feature - what is the feature value?



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Four rectangle Haar feature - what is the feature value?

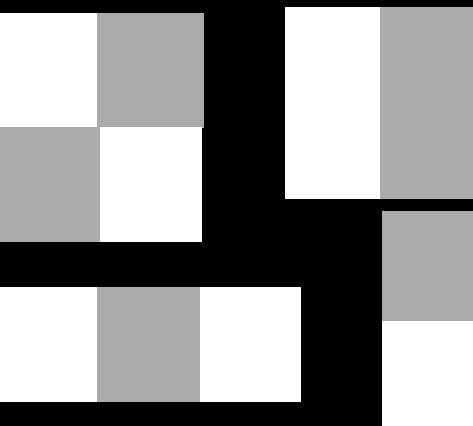


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Fast computing of Haar features



24 x 24 pixels



- Even for small Haar features, there are quite a lot of basic operations
- The larger the Haar feature, the more operations
- We need a fast way to compute Haar features

How many basic operations (plus and minus) are needed to compute the feature?

15

6

9

21

3

I do not know

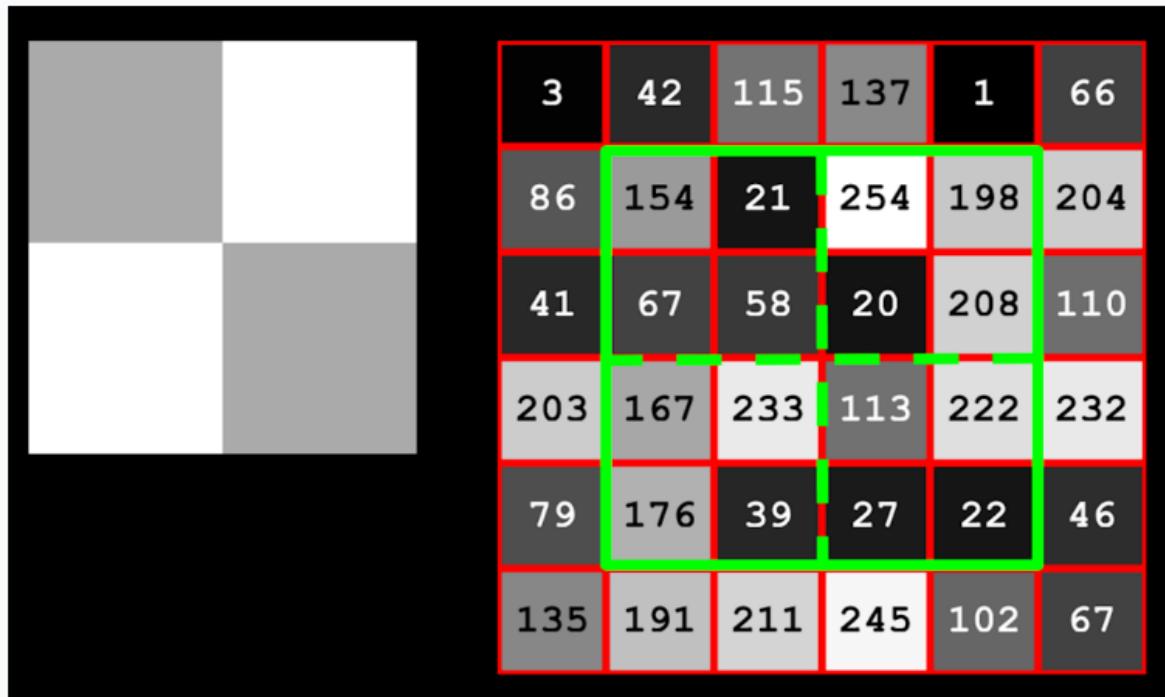
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How many basic operations (plus and minus) are needed to compute the feature?



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How many basic operations (plus and minus) are needed to compute the feature?



15

94%

6

0%

9

6%

21

0%

3

0%

I do not know

0%

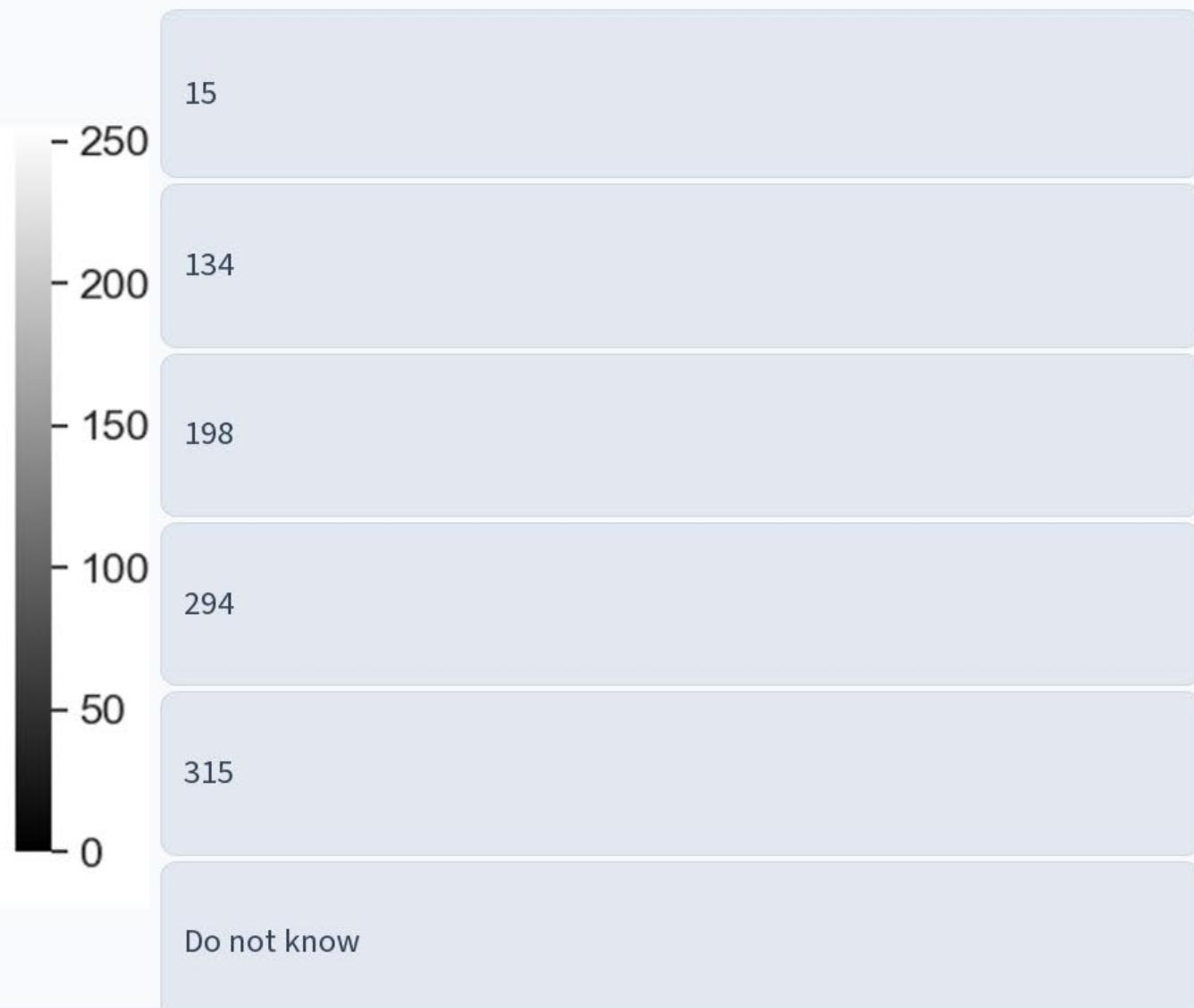
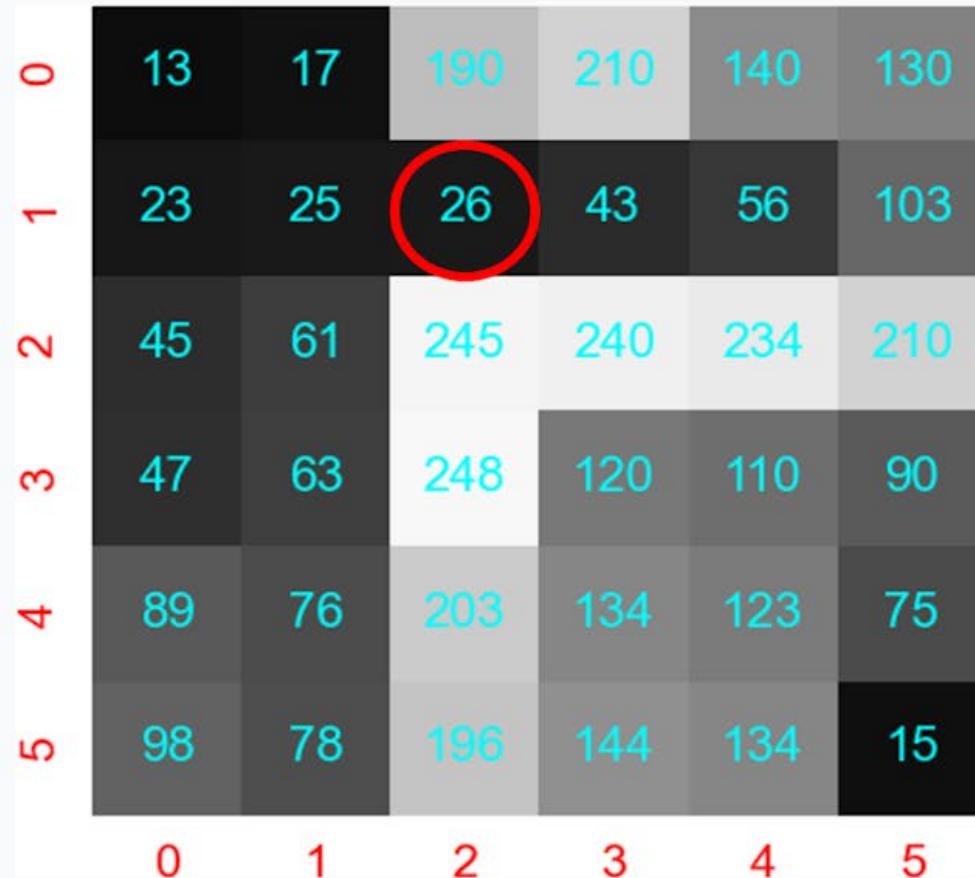
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Fast computation of Haar features – the integral image



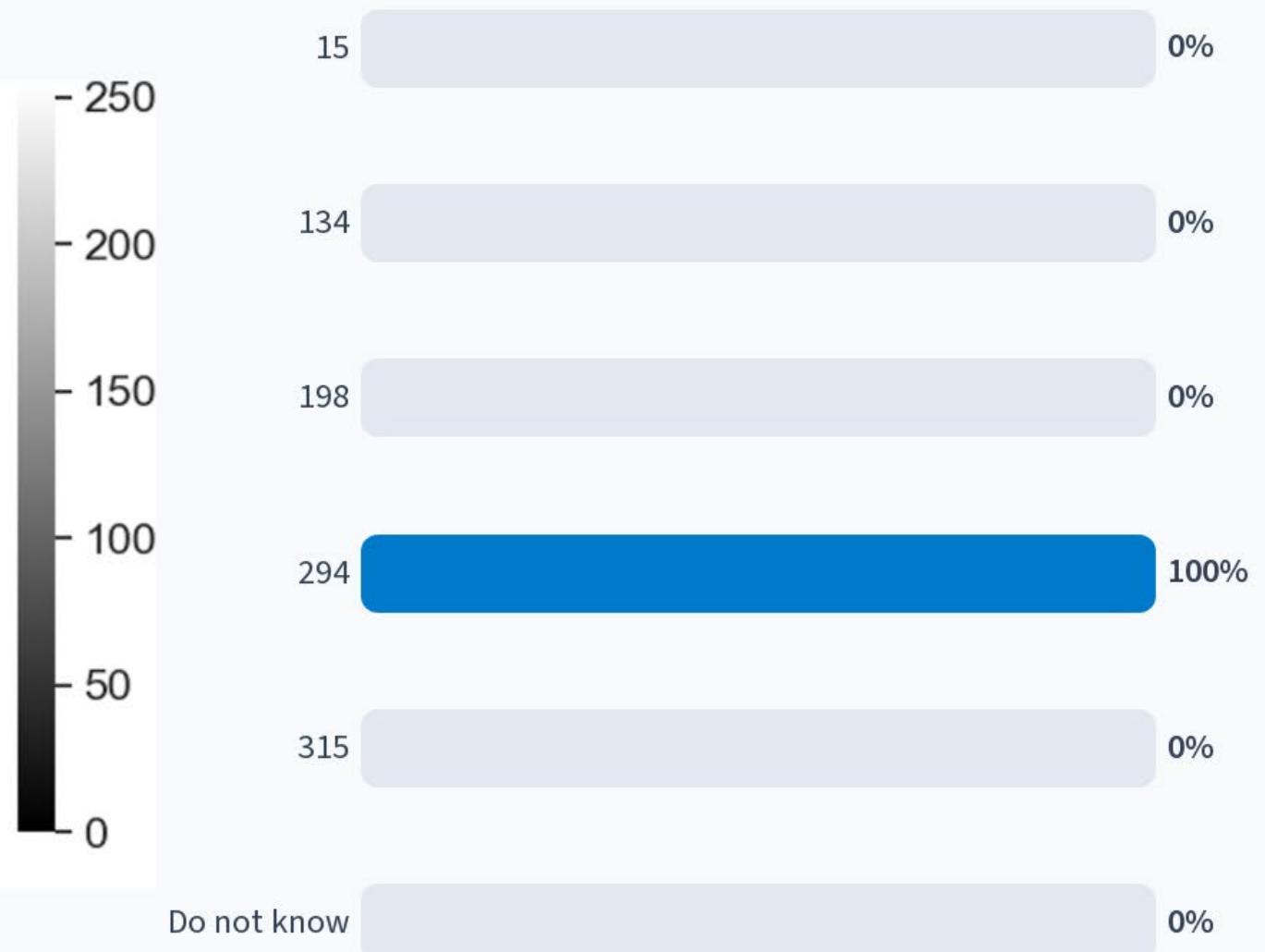
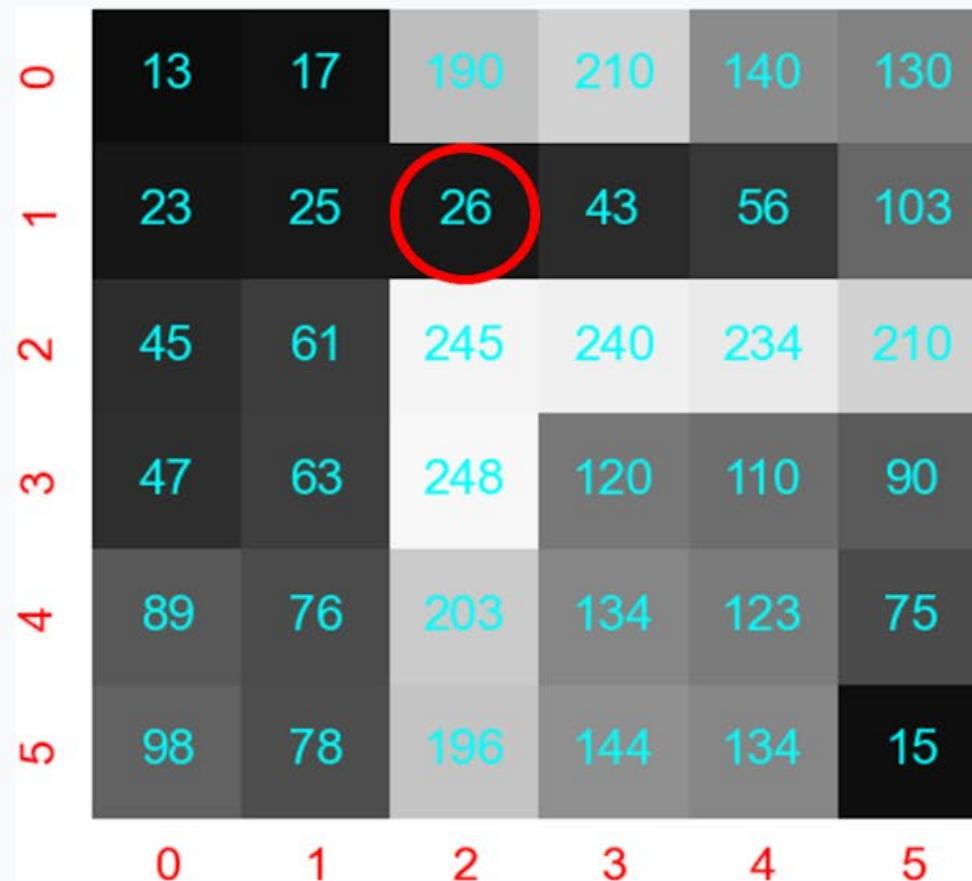
- In an integral image the pixel value is:
 - The sum of pixel above it and to the left of it in the original image
 - Including the pixel itself
- Can be computed very fast

Computing the integral image - what is the value in the marked pixel?



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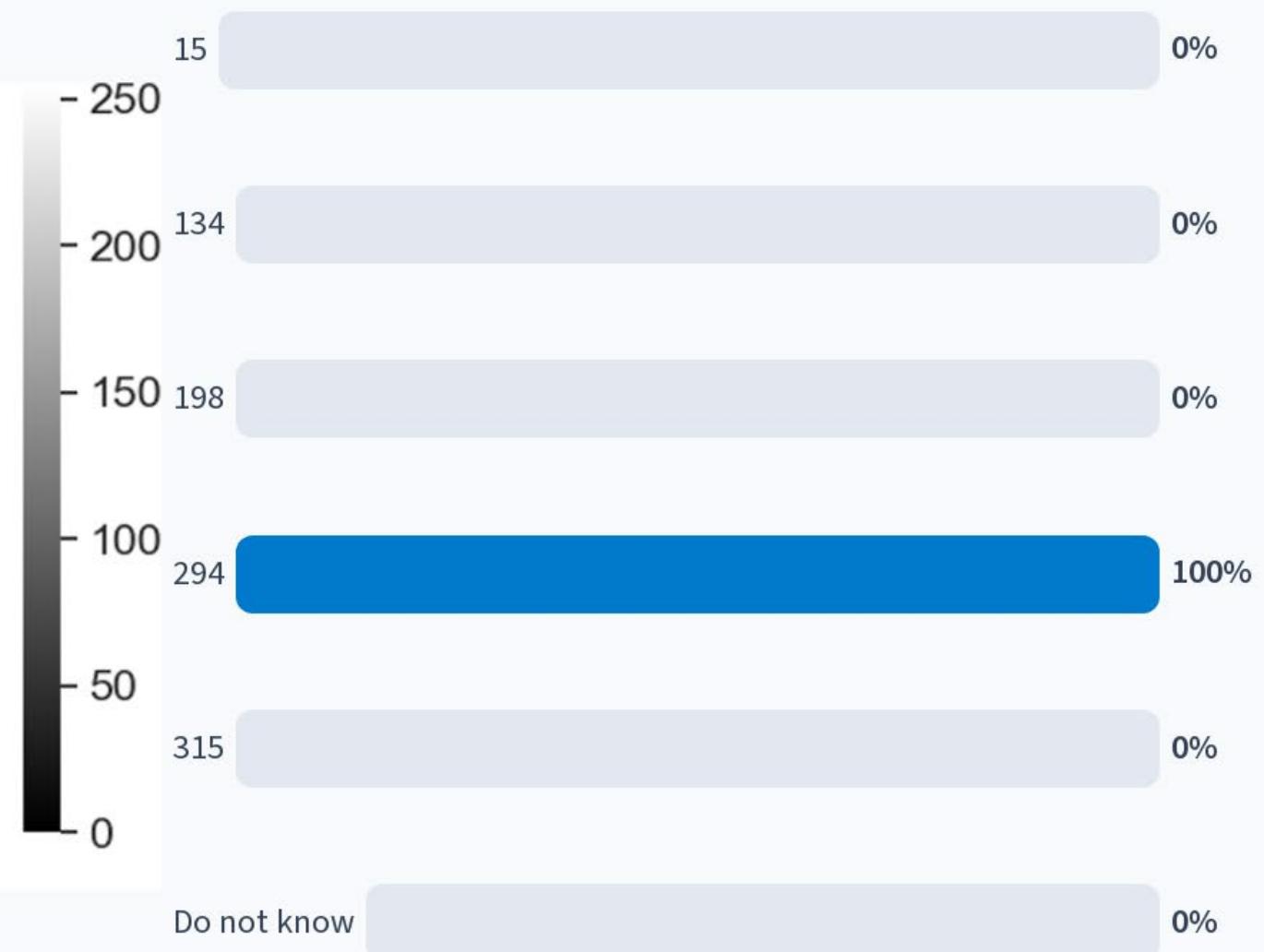
Computing the integral image - what is the value in the marked pixel?



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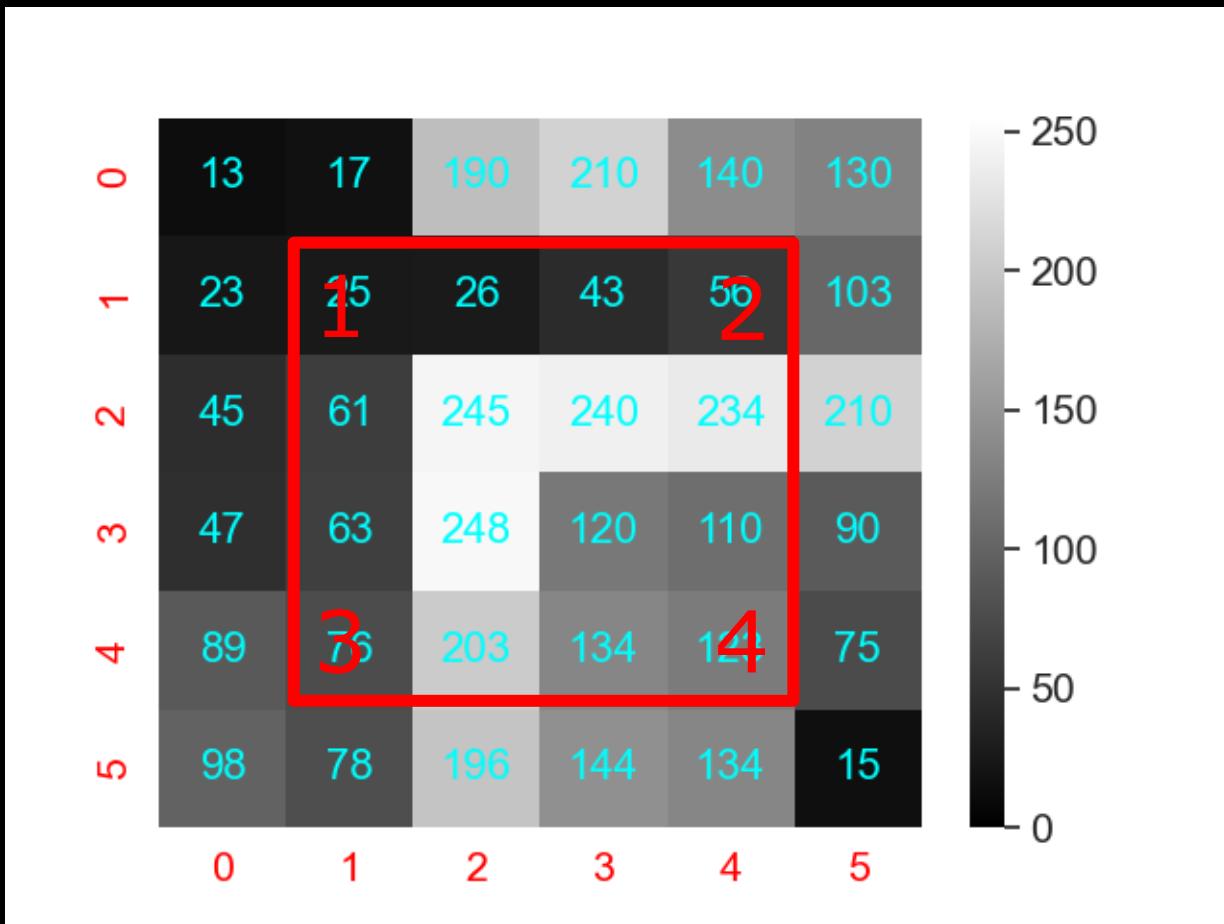
Computing the integral image - what is the value in the marked pixel?

0	13	17	190	210	140	130
1	23	25	26	43	56	103
2	45	61	245	240	234	210
3	47	63	248	120	110	90
4	89	76	203	134	123	75
5	98	78	196	144	134	15
	0	1	2	3	4	5



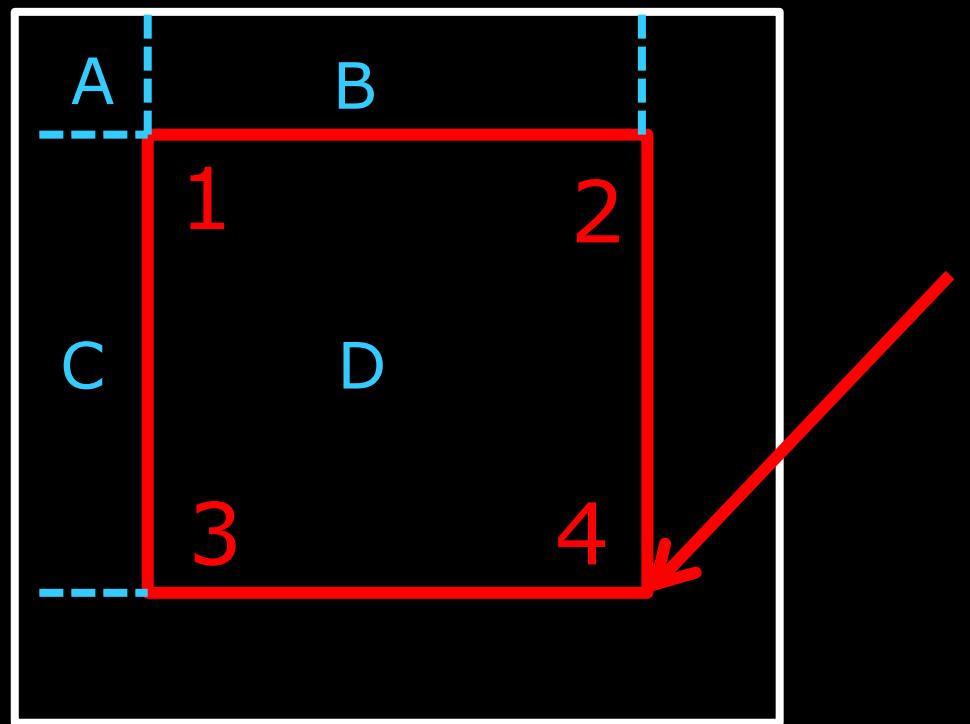
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Using the integral image



- We want to compute the pixel sum in the rectangle
- Defined by four corners: 1, 2, 3, 4

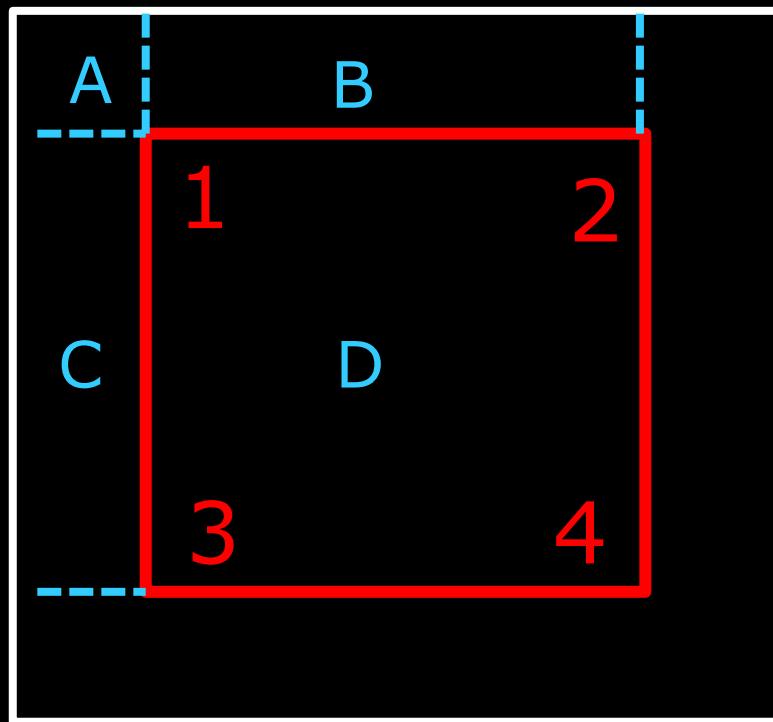
Using the integral image



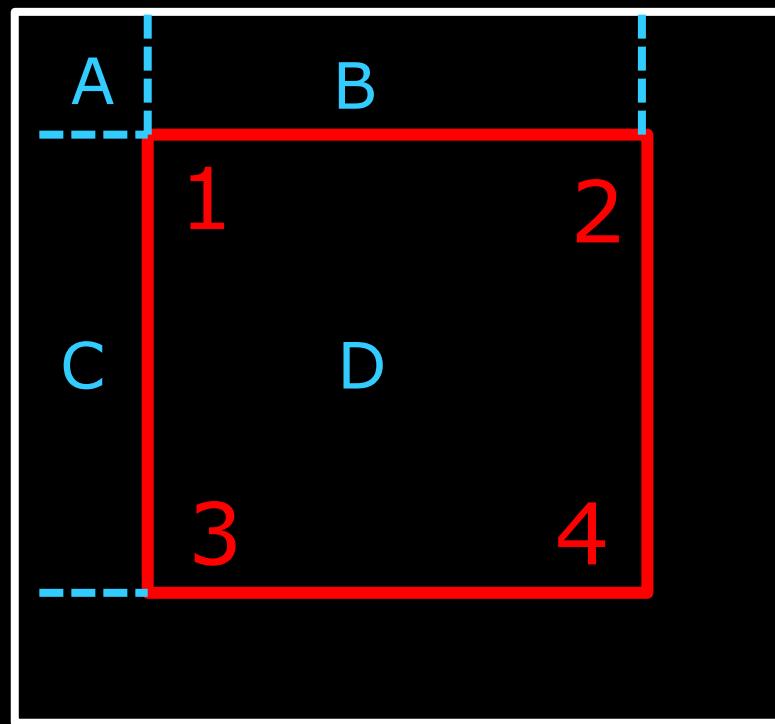
- Define four regions:
 - A, B, C, D
- The sum of pixels in the area
 - $A+B+C+D$ is the value of the integral image at point 4

Using the integral image

- The sum of pixels in the area
 - $A+B$ is the value of the integral image at point 2
 - $A+C$ is the value of the integral image at point 3



Using the integral image – short notation



- The sum of pixels in the area
 - $\text{ii}(2) = A+B$
 - $\text{ii}(3) = A+C$
 - $\text{ii}(4) = A+B+C+D$
 - $\text{ii}(1) = A$
 - $\text{ii}(4)-\text{ii}(3)-\text{ii}(2) = D - A$
- $\text{ii}(4)-\text{ii}(3)-\text{ii}(2)+\text{ii}(1) = D$

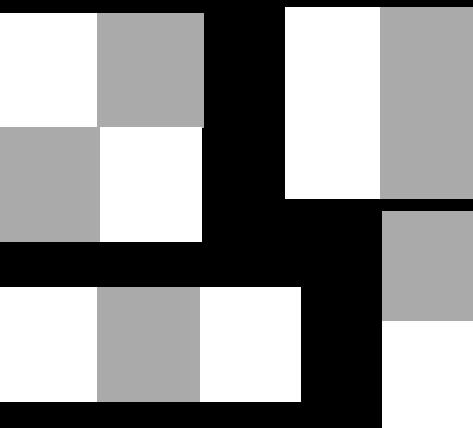
Course evaluation

- Very important to get your feedback on the course
- Please do it now – log into DTU Inside and fill in the evaluation
- What works well – so we should keep it and strengthen that part
- What can be improved and how?
- The question about "The teacher gave me feedback on my progress"
 - Very hard with large courses
 - We try with quizzes, TAs, exercise solutions

Haar features in an image window



24 x 24 pixels



- Image window of 24 x 24 pixels
- All possible sizes and shapes of Haar features
- More than 180.000 features according to Viola and Jones
- They are *overcomplete* – meaning there is a very high redundancy
- We need *feature selection*

Possible features

$$f_1 = \begin{matrix} & \text{white} \\ \text{white} & \begin{matrix} \text{white} & \text{gray} \\ \text{gray} & \text{white} \end{matrix} \end{matrix}$$

$$f_5 = \begin{matrix} & \text{white} & \text{gray} \\ \text{white} & \begin{matrix} \text{gray} & \text{white} \\ \text{white} & \text{white} \end{matrix} \end{matrix}$$

$$f_2 = \begin{matrix} \text{white} & \text{gray} \end{matrix}$$

$$f_6 = \begin{matrix} \text{white} & \text{gray} \\ \text{white} & \text{white} \end{matrix}$$

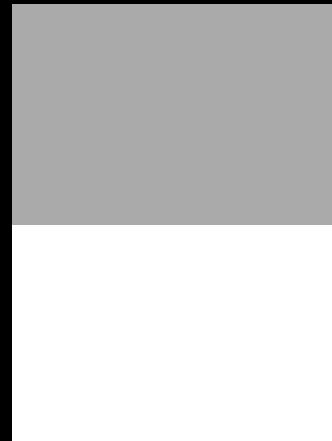
$$f_3 = \begin{matrix} \text{white} & \text{gray} & \text{white} \end{matrix}$$

$$f_7 = \begin{matrix} \text{white} & \text{gray} & \text{white} \\ \text{white} & \text{white} & \text{white} \end{matrix}$$

$$f_4 = \begin{matrix} \text{gray} \\ \text{white} \end{matrix}$$

$$f_8 = \begin{matrix} \text{gray} \\ \text{white} \end{matrix}$$

... $f_{180000} =$



Feature selection – from the article



- There are over 180,000 rectangle features associated with each image sub-window, a number far larger than the number of pixels.
- Even though each feature can be computed very efficiently, computing the complete set is prohibitively expensive.
- Our hypothesis, which is borne out by experiment, is that a very small number of these features can be combined to form an effective classifier.
- The main challenge is to find these features

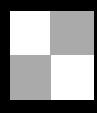


Learning Classification Functions

Weak classifier

 $x =$ 

24 x 24 sub-window

 $f_j =$ 

Feature value computed on the sub-window

 $p_j \in [-1, 1]$

Parity – determines if the feature value should be positive or negative

 θ_j

Feature threshold

Weak classifier

$$h_j(x) = \begin{cases} 1 & \text{if } p_j f_j(x) < p_j \theta_j \\ 0 & \text{otherwise} \end{cases}$$

$$x = \boxed{\text{Image of a person's arm}} \quad f_j(\boxed{\text{Image of a person's arm}}) = \boxed{\text{Image of a person's arm with a 3x3 grid overlay}} = 2049$$

Learnt by training: $p_j = 1 \quad \theta_j = 456$

$$\rightarrow 1 * 2049 < 1 * 456 \rightarrow h_j(\boxed{\text{Image of a person's arm}}) = 0$$

What is this parity?

$$h_j(x) = \begin{cases} 1 & \text{if } p_j f_j(x) < p_j \theta_j \\ 0 & \text{otherwise} \end{cases}$$

Weak classifier

$$x = \boxed{\text{Image of a person's arm}} \quad f_j(\boxed{\text{Image of a person's arm}}) = \boxed{\text{Image of a person's arm with a 3x3 gray mask}} = 2049$$

Learnt by training: $p_j = -1 \quad \theta_j = 456$

$$\rightarrow -1 * 2049 < -1 * 456 \rightarrow h_j(\boxed{\text{Image of a person's arm}}) = 1$$

Creating a strong classifier from weak classifiers

$$h(x) = \begin{cases} 1 & \sum_{t=1}^T \alpha_t h_t(x) \geq \frac{1}{2} \sum_{t=1}^T \alpha_t \\ 0 & \text{otherwise} \end{cases}$$

$$h_1(\boxed{\text{ }}) = \boxed{\text{ }} \quad \text{A small image of a person's face with a 2x2 grid of squares overlaid on it. The top-left square is white, the top-right is gray, the bottom-left is gray, and the bottom-right is white. A blue box surrounds the entire image.}$$

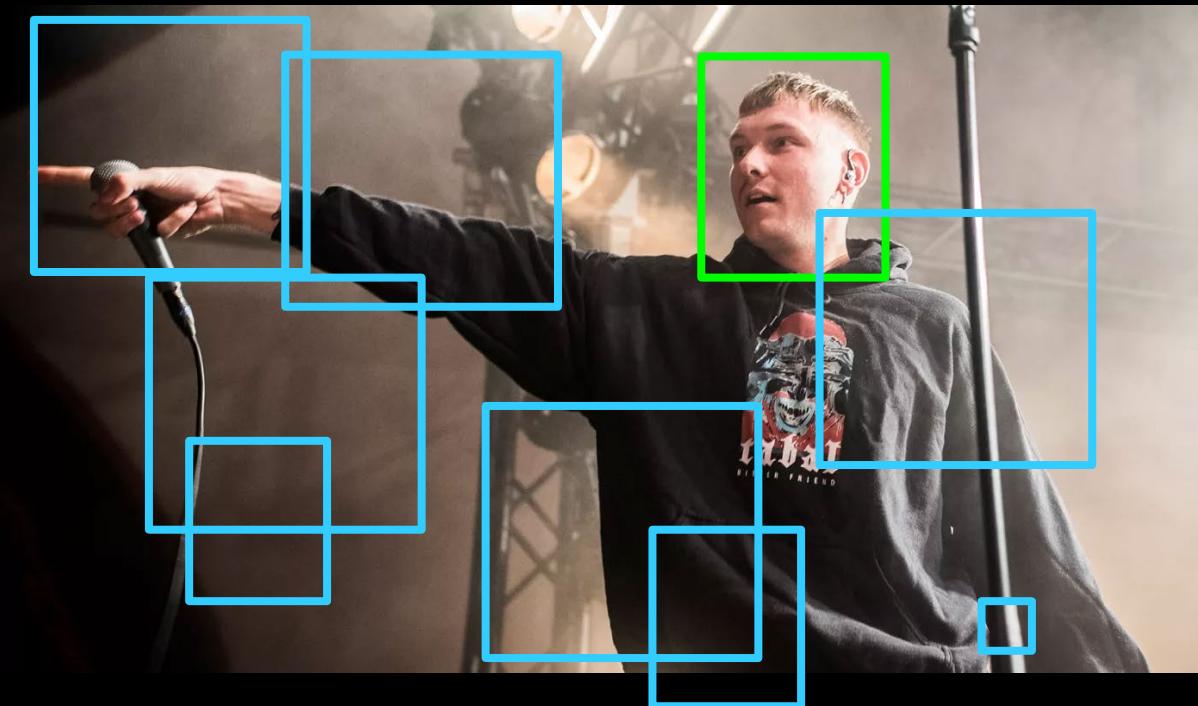
$$h_2(\boxed{\text{ }}) = \boxed{\text{ }} \quad \text{A small image of a person's face with a 2x2 grid of squares overlaid on it. The top-left square is white, the top-right is gray, the bottom-left is white, and the bottom-right is white. A blue box surrounds the entire image.}$$

...

$$h(\boxed{\text{ }}) = \alpha_1 h_1 + \alpha_2 h_2 + \cdots + \alpha_T h_T$$

Learnt using AdaBoost

Boosted features – good performance but not enough



- Frontal face classifier with
 - $T=200$ features
 - Detection rate 95%
 - False positives 1 in 14084
 - 0.7 seconds for a 384×288

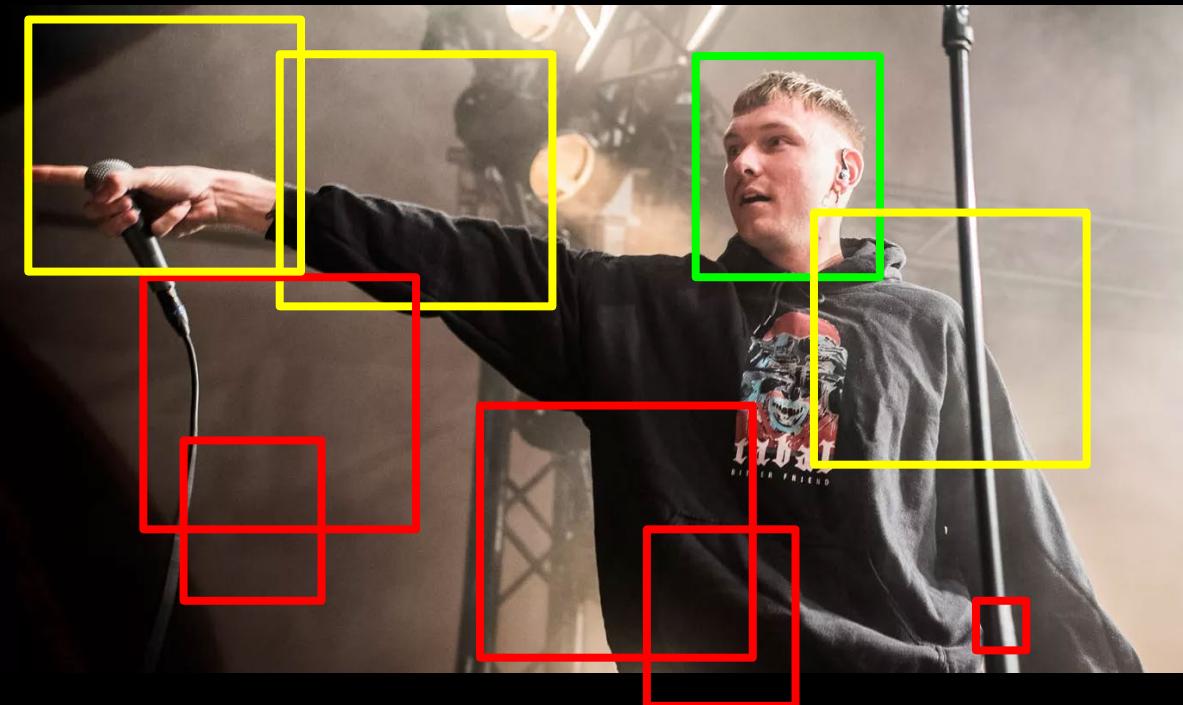
$$h_1(\boxed{}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

The Attentional Cascade



Image Attention

- The process of focusing on specific parts of an image
 - Followed by fine grained analysis of selected windows



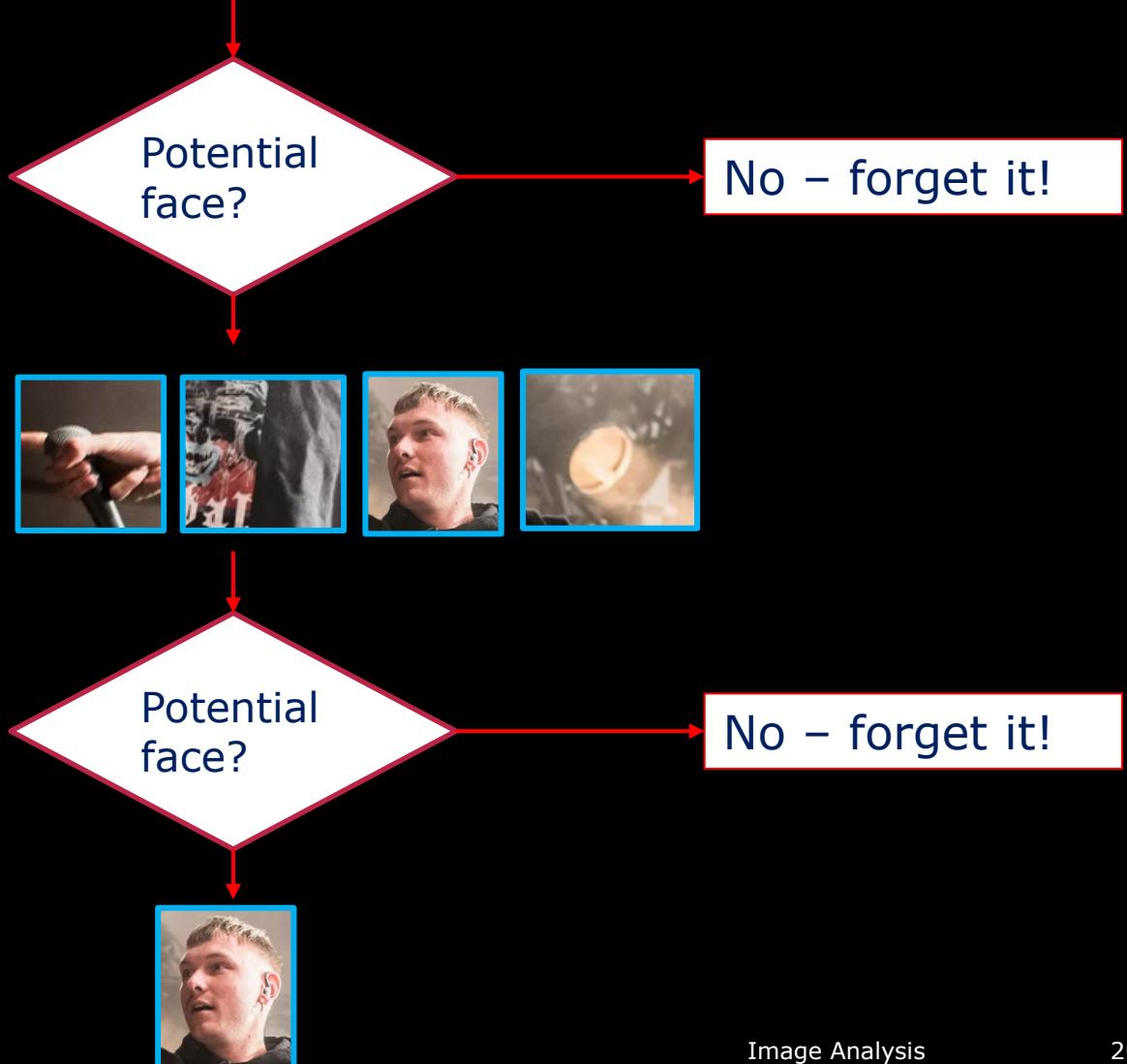
Focusing on potential face regions

Cascaded classifier



Also called a *degenerate decision tree*

Input image windows



What is a false negative?

A face window classified as face window

A background window classified as a face window

A face window classified as a background window

A background window classified as a background window

I do not know

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What is a false negative?

A face window classified as face window

0%

A background window classified as a face window

22%

A face window classified as a background window 

78%

A background window classified as a background window

0%

I do not know

0%

Start the presentation to see live content. For screen share software, share the entire screen. Get help at pollev.com/app

What is a false negative?

A face window classified as face window

0%

A background window classified as a face window

22%

A face window classified as a background window 

78%

A background window classified as a background window

0%

I do not know

0%

Start the presentation to see live content. For screen share software, share the entire screen. Get help at pollev.com/app

The attentional cascade



- Quickly reject negative sub-windows
 - Detect almost all positive sub-windows
 - False-negatives close to zero
 - Keep all potential face windows
 - Using the training set to find weights that fulfills this criterion



- Later more complex classifier
 - Low false positive rate



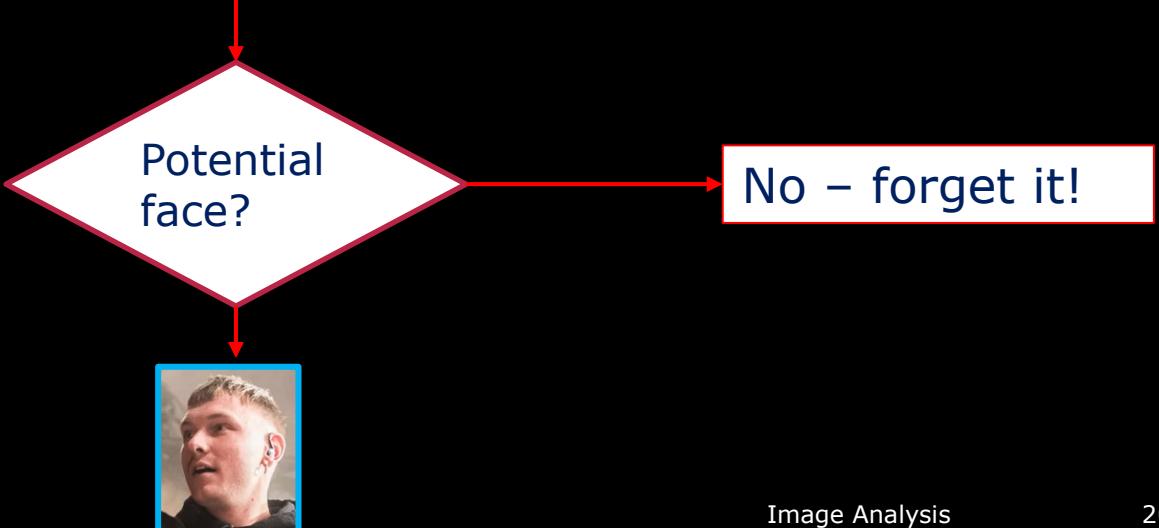
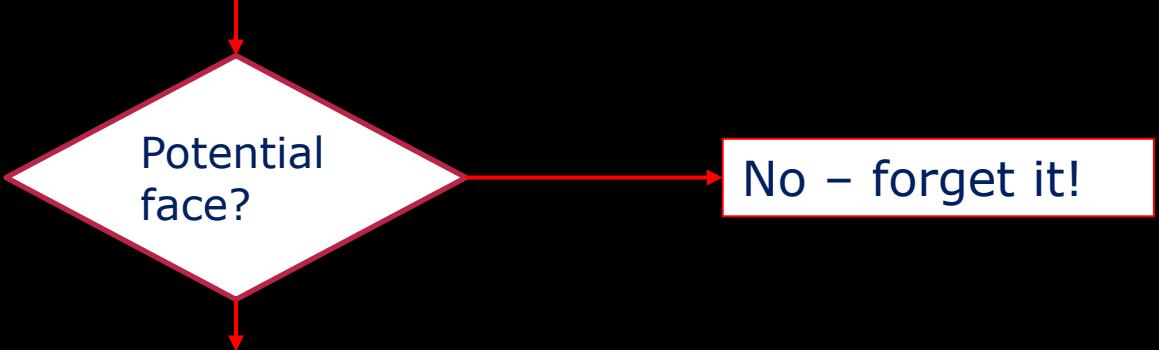
Training a cascade

$$h(\boxed{\text{ }}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

Learnt using AdaBoost

$$h(\boxed{\text{ }}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

Learnt using AdaBoost



First stage classifier

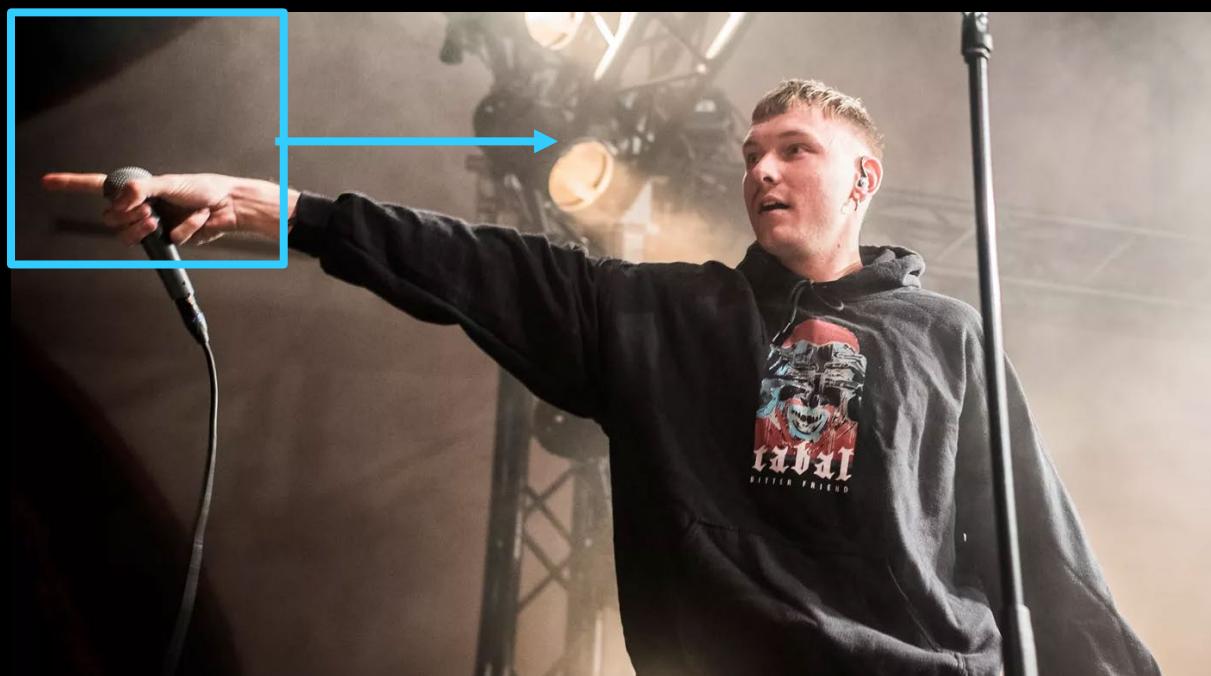


Final classifier



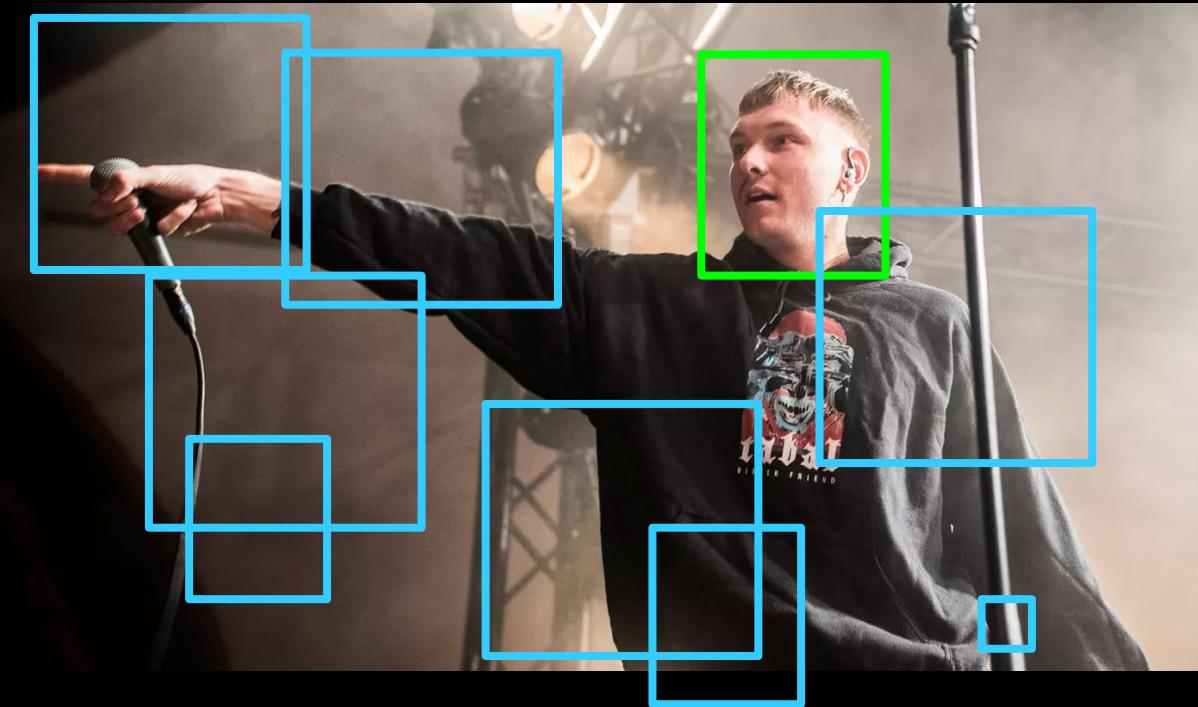
- 38 stages (step in the cascade)
- Total 6000 features (over the entire cascade)
- Faces are detected using on average 10 features per sub-window

Finding all faces in an image



- Slide a sub-window over the entire image
- Do a face detection for all positions
- Scale the features in a certain interval
 - To find faces of different sizes

Conclusion



- One of the most important algorithms before deep learning
- Uses many interesting concepts
 - Attention
 - Boosted weak classifiers
 - Very fast feature computation

Demo

Next week(s)

- Statistical models of shape and appearance